# $\sigma$ - and $\pi$-Bond Strengths in Main Group 3-5 Compounds 

Daniel J. Grant and David A. Dixon*<br>Department of Chemistry, Shelby Hall, The University of Alabama, P.O. Box 870336, Tuscaloosa, Alabama 35487-0336

Received: August 7, 2006; In Final Form: September 7, 2006


#### Abstract

The $\sigma$ - and $\pi$-bond strengths for the molecules $\mathrm{BH}_{2} \mathrm{NH}_{2}, \mathrm{BH}_{2} \mathrm{PH}_{2}, \mathrm{AlH}_{2} \mathrm{NH}_{2}$, and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ have been calculated by using ab initio molecular electronic structure theory at the $\operatorname{CCSD}(\mathrm{T}) / \mathrm{CBS}$ level. The adiabatic $\pi$-bond energy is defined as the rotation barrier between the equilibrium ground-state configuration and the $C_{s}$ symmetry transition state for torsion about the $\mathrm{A}-\mathrm{X}$ bond. We also report instrinsic $\pi$-bond energies corresponding to the adiabatic rotation barrier corrected for the inversion barrier at N or P . The adiabatic $\sigma$-bond energy is defined as the dissociation energy of $\mathrm{AH}_{2} \mathrm{XH}_{2}$ to $\mathrm{AH}_{2}+\mathrm{XH}_{2}$ in their ground states minus the adiabatic $\pi$-bond energy. The adiabatic $\sigma$-bond strengths for the molecules $\mathrm{BH}_{2} \mathrm{NH}_{2}, \mathrm{BH}_{2} \mathrm{PH}_{2}, \mathrm{AlH}_{2} \mathrm{NH}_{2}$, and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ are $109.8,98.8,77.6$, and $68.3 \mathrm{kcal} / \mathrm{mol}$, respectively, and the corresponding adiabatic $\pi$-bond strengths are $29.9,10.5,9.2$, and $2.7 \mathrm{kcal} / \mathrm{mol}$, respectively.


## Introduction

The suitability of $\mathrm{NH}_{x} \mathrm{BH}_{x}(x=1-4)$ compounds for hydrogen storage has recently been evaluated using theoretical methods. ${ }^{1-3}$ The calculations showed that $\mathrm{BH}_{3} \mathrm{NH}_{3}(\mathrm{~g}), \mathrm{BH}_{3}-$ $\mathrm{NH}_{3}(\mathrm{~s})$, and $\left[\mathrm{BH}_{4}^{-}\right]\left[\mathrm{NH}_{4}{ }^{+}\right]$(s) can potentially serve as hydrogen storage systems based on the thermodynamics. In addition, molecular systems isoelectronic to the amine boranes were studied computationally as alternative candidates for $\mathrm{H}_{2}$ storage systems. ${ }^{4}$ On the basis of the calculated heats of formation, $\mathrm{AlH}_{3} \mathrm{NH}_{3}(\mathrm{~g}),\left[\mathrm{AlH}_{4}^{-}\right]\left[\mathrm{NH}_{4}{ }^{+}\right](\mathrm{s}), \mathrm{AlH}_{3} \mathrm{PH}_{3}(\mathrm{~g}),\left[\mathrm{AlH}_{4}^{-}\right]\left[\mathrm{PH}_{4}^{+}\right](\mathrm{s})$, and $\left[\mathrm{BH}_{4}^{-}\right]\left[\mathrm{PH}_{4}^{+}\right](\mathrm{s})$ have the potential to serve as $\mathrm{H}_{2}$ storage systems in terms of the reaction energetics for $\mathrm{H}_{2}$ release.

We are interested in the chemistry of these species in terms of their stability and reactivity. Because of the novel electronic structure of these species, we are interested in their bond energies. We previously have provided the best estimates of the Lewis acid-base donor-acceptor $\sigma$-bond strengths in $\mathrm{AH}_{3}-$ $\mathrm{XH}_{3}$ compounds as shown in Table 1. ${ }^{3,4}$ These values are quite low as compared to a covalent $\mathrm{C}-\mathrm{C} \sigma$-bond energy, for example, the value of $90.1 \mathrm{kcal} / \mathrm{mol}$ at 298 K for $\mathrm{C}_{2} \mathrm{H}_{6}{ }^{5}$ The $\mathrm{AH}_{3} \mathrm{XH}_{3}$ molecules can eliminate $\mathrm{H}_{2}$ to form $\mathrm{AH}_{2} \mathrm{XH}_{2}$ molecules. The resulting $\mathrm{AH}_{2} \mathrm{XH}_{2}$ molecules have $\sigma$-bonds formed between the $\mathrm{AH}_{2}$ and $\mathrm{XH}_{2}$ groups with approximate $\mathrm{sp}^{2}-\mathrm{sp}^{2}$ hybridization and $\pi$-bonds formed by donation of the lone pair on the Group VA $\mathrm{XH}_{2}$ group to the vacant p orbital on the Group IIIA $\mathrm{AH}_{2}$ group. The strengths of the $\pi$-bond and the resulting $\sigma$-bond are questions that need to be addressed. We are particularly interested in the inherent bond energies of the $\sigma$ - and $\pi$-bonds to better understand the thermodynamic driving forces for $\mathrm{H}_{2}$ release. The bond energies in these systems can be compared to the $\sigma$ - and $\pi$-bond strengths in $\mathrm{C}_{2} \mathrm{H}_{4}$, which has a covalent $\pi$ bond. ${ }^{6}$

Several methods exist in the literature for determining $\pi$-bond strengths. A general procedure is to compare the bond dissociation energies of double, $D^{\circ}(\mathrm{X}=\mathrm{Y})$, and single, $D^{\circ}(\mathrm{X}-\mathrm{Y})$, bonds. The issue here is the proper description of how to define the $\pi$-bond energy. ${ }^{7-9}$ One method involves the use of hydrogenation thermochemical cycles and bond dissociation energies. The energy required to dehydrogenate a singly bonded

TABLE 1: Donor $\boldsymbol{\sigma}$-bond Strengths in $\mathbf{A H}_{3} \mathbf{X H}_{3}$ Compounds ${ }^{a}$

| molecule | $\sigma$-bond energy <br> $(0 \mathrm{~K})$ | $\sigma$-bond energy <br> $(298 \mathrm{~K})$ |
| :---: | :---: | :---: |
| $\mathrm{H}_{3} \mathrm{BNH}_{3}{ }^{b}$ | 25.9 | 27.2 |
| $\mathrm{H}_{3} \mathrm{AlNH}_{3}{ }^{c}$ | 26.1 | 27.3 |
| $\mathrm{H}_{3} \mathrm{BPH}_{3}{ }^{c}$ | 21.1 | 22.5 |
| $\mathrm{H}_{3} \mathrm{AlPH}_{3}{ }^{c}$ | 14.0 | 14.7 |
| ${ }^{a}$ In kcal/mol. ${ }^{b}$ Ref $3 .{ }^{c}$ Ref 4. |  |  |

compound to produce a double bond can be used to estimate the strength of the double bond provided that the overall heat of the dehydrogenation reaction and the bond dissociation energies are known. ${ }^{6,10}$ One also can look at the barrier to rotation about the $\mathrm{A}-\mathrm{X}$ bond as rotation about the $\sigma$-bond by $90^{\circ}$ breaks the $\pi$-bond interaction of the molecule. This can be done, for example, by measuring the kinetics for cis-trans isomerization. ${ }^{11}$ Borden ${ }^{7}$ has discussed various approaches to calculating the $\pi$-bond energy in olefins and has shown that relaxation of the orthogonal diradical is important in determining the $\pi$ bond energy in $\mathrm{C}_{2} \mathrm{~F}_{4}$ as compared to $\mathrm{C}_{2} \mathrm{H}_{4}$ as well as issues related to diabatic (dissociation to the configuration most closely representing the bonding configuration in the molecule) vs adiabatic (dissociation to the ground state of the separated species) dissociation energies. Carter and Goddard have provided a similar discussion for substituted olefins. ${ }^{8}$
To calculate the $\sigma$-bond energy, one has to evaluate the $\pi$ bond strength. We have chosen to use the rotation barrier approach as the hydrogenation method could lead to very different types of radicals than those found in carbon-based systems, and it is not possible to determine which end to hydrogenate first. We can write the following process:

$$
\begin{align*}
& \mathrm{H}_{2} \mathrm{~A}=\mathrm{XH}_{2} \rightarrow \cdot{ }^{\bullet} \mathrm{AH}_{2}+{ }^{\bullet} \mathrm{XH}_{2} \\
& \quad \Delta H(0 \mathrm{~K})=\sigma \text {-bond }+\pi \text {-bond } \tag{1}
\end{align*}
$$

where A is the Group 3A atom and X is the group 5A atom. The total dissociation energy for this reaction is the sum of the $\sigma$ - and $\pi$-bond energies. Given the energies of the three species,
one can calculate the sum of the $\sigma$ - and $\pi$-bond energies. The sum of the bond energies at the adiabatic limit is for dissociation to the ground states, which are ${ }^{2} \mathrm{~A}_{1}$ for $\mathrm{AH}_{2}$ (orbital with unpaired electron in the plane) and ${ }^{2} \mathrm{~B}_{1}$ for $\mathrm{XH}_{2}$ (orbital with unpaired electron out of the plane and orbital with the lone pair in the plane). To calculate the $\pi$ bond energy, one can rotate about the $\mathrm{A}-\mathrm{X}$ bond by $90^{\circ}$ so that there is no interaction between the lone pair on the $\mathrm{XH}_{2}$ with the vacant orbital on $\mathrm{AH}_{2}$.

$$
\begin{equation*}
\mathrm{H}_{2} \mathrm{~A}=\mathrm{XH}_{2} \rightarrow \mathrm{H}_{2} \mathrm{~A}-\mathrm{XH}_{2} \quad \Delta H(0 \mathrm{~K})=\pi \text {-bond } \tag{2}
\end{equation*}
$$

In $\mathrm{C}_{2} \mathrm{H}_{4}$, this is equivalent to breaking the covalent interaction between the p orbitals and to putting one electron on each $\mathrm{CH}_{2}$ group to form a diradical. For the Group 3-5 binary compounds $\mathrm{H}_{2} \mathrm{~A}=\mathrm{XH}_{2}$ with $\mathrm{A}=\mathrm{B}, \mathrm{Al}$ and $\mathrm{X}=\mathrm{N}, \mathrm{P}$ the rotation process stays on the closed shell singlet potential energy surface so that there is no need to be concerned with accessing an open shell species. In the rotated structure, the pair of electrons involved in the rotation localize as the lone pair on the Group 5A atom. An issue that arises in these compounds is the structure in the rotated state.

There have been several previous theoretical studies of the $\sigma$ - and $\pi$-bond energies of the molecules presented here. Allen and Fink ${ }^{12}$ predicted that aminoborane, $\mathrm{BH}_{2} \mathrm{NH}_{2}$, has two rotational transition states at the CISD $+\mathrm{Q} / \mathrm{DZ}+\mathrm{P}$ level, one of $C_{s}$ symmetry at $32.4 \mathrm{kcal} / \mathrm{mol}$ and one of $C_{2 v}$ symmetry at 37.9 $\mathrm{kcal} / \mathrm{mol}$, both with respect to the planar ground-state configuration. This type of energy difference is consistent with relaxation of the geometry in the rotated structure as discussed by Borden ${ }^{7}$ as well as the size of the inversion barrier in $\mathrm{NH}_{3} .{ }^{13}$ McKee ${ }^{14}$ predicted the rotational barrier in $\mathrm{BH}_{2} \mathrm{NH}_{2}$ to be 32.1 $\mathrm{kcal} / \mathrm{mol}$ at the MP4/6-31+G(2d,p) level of theory. Allen et al. ${ }^{15}$ and Allen and Fink ${ }^{16}$ also investigated the internal rotational energy barrier of borylphosphine at the level described above. They predicted that the $\mathrm{BH}_{2} \mathrm{PH}_{2}$ molecule can undergo internal rotation through either a low-energy transition state of $C_{s}$ symmetry $10.0 \mathrm{kcal} / \mathrm{mol}$ above the ground-state structure or a high-energy transition state of $C_{2 v}$ symmetry, $46.4 \mathrm{kcal} / \mathrm{mol}$ above the ground state. The difference in the two rotation barriers is consistent with the inversion barrier in $\mathrm{PH}_{3} .{ }^{17}$ Coolidge and Borden ${ }^{18}$ also have studied the rotation barrier in $\mathrm{BH}_{2} \mathrm{PH}_{2}$ and found a barrier of $10.4 \mathrm{kcal} / \mathrm{mol}$ passing through a $C_{s}$ transition state and a barrier of $44.6 \mathrm{kcal} / \mathrm{mol}$ passing through a $C_{2 v}$ rotated structure at the MP4 level. For alane amine, $\mathrm{AlH}_{2} \mathrm{NH}_{2}$, Fink et al. ${ }^{19}$ predicted the rotational energy barrier to be $11.2 \mathrm{kcal} / \mathrm{mol}$ at the RHF/6-31+G** level. Davy and Jaffrey ${ }^{20}$ obtained a value of $11.0 \mathrm{kcal} / \mathrm{mol}$ for the rotational barrier energy of $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ at the HF/DZP level.

We use the approach developed for accurate molecular thermochemistry ${ }^{21}$ and for the heats of formation of the parent compounds ${ }^{3,4}$ to predict the bond energies. This approach is based on calculating the total atomization energy of a molecule and using this with known heats of formation of the atoms to calculate the heat of formation at 0 K . The approach starts with the coupled cluster theory with single and double excitations and includes a perturbative triples correction $(\operatorname{CCSD}(\mathrm{T})),{ }^{22-24}$ combined with the correlation-consistent basis sets ${ }^{25,26}$ extrapolated to the complete basis set limit to treat the correlation energy of the valence electrons. This is followed by a number of smaller additive corrections including core-valence interactions and relativistic effects, both scalar and spin-orbit. Finally, one must include the zero point energy obtained either from experiment, theory, or some combination. Corrections to 298 K then can be calculated by using standard thermodynamic and statistical
mechanics expressions in the rigid rotor-harmonic oscillator approximation ${ }^{27}$ and appropriate corrections for the heat of formation of the atoms. ${ }^{28}$

## Computational Approach

We used the augmented correlation consistent basis sets aug-cc-pVnZ for $\mathrm{H}, \mathrm{B}$, and $\mathrm{N}(n=\mathrm{D}, \mathrm{T}, \mathrm{Q}){ }^{25,26}$ For the sake of brevity, we abbreviate the names to aVnZ. Only the spherical components ( $5 \mathrm{~d}, 7 \mathrm{f}$, and 9 g ) of the Cartesian basis functions were used. All of the current work was performed with the MOLPRO suite of programs. ${ }^{29}$ The open-shell $\operatorname{CCSD}(\mathrm{T})$ calculations for the atoms were carried out at the R/UCCSD(T) level. In this approach, a restricted open shell HartreeFock (ROHF) calculation was initially performed and the spin constraint was relaxed in the coupled cluster calculation. ${ }^{30-32}$ All of the calculations were done on a massively parallel HP Linux cluster with 1970 Itanium-2 processors in the Molecular Sciences Computing Facility in the William R. Wiley Environmental Molecular Sciences Laboratory or on the 144 processor Cray XD-1 computer system at the Alabama Supercomputer Center.

The geometries were optimized numerically at the frozen core $\operatorname{CCSD}(T)$ level with the aug-cc-pVDZ and aug-cc-pVTZ correlation-consistent basis sets. The CCSD(T)/aug-cc-pVTZ geometries were then used in single point $\operatorname{CCSD}(\mathrm{T}) /$ aug-ccpVQZ calculations. For the planar and rotated $C_{2 v}$ structures, geometry optimizations only were done at the $\operatorname{CCSD}(\mathrm{T}) /$ aug-cc-pVDZ level as the energies of the ground state structure or the lowest energy rotated structure only decreased by a few tenths of a $\mathrm{kcal} / \mathrm{mol}$ upon optimization at the $\operatorname{CCSD}(\mathrm{T}) /$ aug-cc-pVTZ level. All of the vibrational frequencies were calculated at the MP2/cc-pVTZ level ${ }^{33}$ using the Gaussian program system. ${ }^{34}$ These were used for the zero point energies and for the thermal corrections and entropies.

It recently has been found that tight d functions are necessary for calculating accurate atomization energies for 2 nd row elements, ${ }^{35}$ so we also included additional tight d functions in our calculations. Basis sets containing extra tight d functions are denoted aug-cc-pV $(n+\mathrm{d}) \mathrm{Z}$ in analogy to the original augmented correlation consistent basis sets. We use aug-cc$\mathrm{pV}(n+\mathrm{d}) \mathrm{Z}$ to represent the combination of aug-cc-pV $(n+\mathrm{d}) \mathrm{Z}$ (on the 2nd row atoms Al and P) and aug-cc-pVnZ (on H, B, and N ) basis sets and abbreviate this as $\mathrm{aV}(n+\mathrm{d}) \mathrm{Z}$. The CCSD(T) total energies were extrapolated to the CBS limit by using a mixed exponential/Gaussian function of the form:

$$
\begin{equation*}
E(n)=E_{\mathrm{CBS}}+A \exp [-(n-1)]+B \exp \left[-(n-1)^{2}\right] \tag{3}
\end{equation*}
$$

with $n=2(\mathrm{DZ}), 3(\mathrm{TZ})$ and $4(\mathrm{QZ})$, as first proposed by Peterson et al. ${ }^{36}$ This extrapolation method has been shown to yield atomization energies in the closest agreement with experiment (by a small amount) as compared to other extrapolation approaches up through $n=4$.

Core-valence corrections, $\Delta E_{\mathrm{CV}}$, were obtained at the CCSD-(T)/cc-pwCVTZ level of theory. ${ }^{37}$ Scalar relativistic corrections $\left(\Delta E_{\mathrm{SR}}\right)$, which account for changes in the relativistic contributions to the total energies of the molecule and the constituent atoms, were included at the $\mathrm{CI}-\mathrm{SD}$ (configuration interaction singles and doubles) level of theory using the cc-pVTZ basis set. $\Delta \mathrm{E}_{\text {SR }}$ is taken as the sum of the mass-velocity and 1-electron Darwin (MVD) terms in the Breit-Pauli Hamiltonian. ${ }^{38}$ Most calculations using available electronic structure computer codes do not correctly describe the lowest energy spin multiplet of an atomic state as spin-orbit in the atom is usually not included. Instead, the energy is a weighted average of the available multiplets. For N or P in the ${ }^{4} \mathrm{~S}$ state, no spin-orbit correction

TABLE 2: Optimized $\operatorname{CCSD}(\mathbf{T})$ Bond Lengths $(\AA)$ and Bond Angles $\left({ }^{\circ}\right)$ for the Rotated Structures of $\mathbf{A H}_{2} \mathbf{X H}_{2}$ in $C_{s}$ and $\boldsymbol{C}_{2 v}$ Symmetries

| molecule | basis set | $R_{\text {XH }}$ | $\angle \mathrm{HXH}$ | $\angle \mathrm{HXA}$ | $R_{\text {AH }}$ | $\angle \mathrm{HAH}$ | $\angle \mathrm{HAX}$ |
| :--- | :---: | :---: | ---: | ---: | ---: | ---: | ---: |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}$ (rot) | aVDZ | 1.0308 | 101.34 | 108.25 | 1.2172 | 118.63 | 122.22 |
|  | aVTZ | 1.0218 | 101.86 | 108.87 | 1.2032 | 118.58 | 122.12 |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}$ (rot-planar) | aVDZ | 1.0124 | 113.64 | 123.18 | 1.2475 | 117.36 | 121.32 |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ (rot) | aVDZ | 1.4418 | 90.76 | 91.85 | 1.2067 | 119.00 | 120.77 |
|  | aVTZ | 1.4277 | 90.71 | 91.87 | 1.1920 | 119.13 | 120.62 |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ (rot-planar) | aVDZ | 1.4009 | 115.20 | 122.40 | 1.2044 | 119.65 | 120.17 |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ (rot) | aVDZ | 1.0222 | 105.84 | 118.61 | 1.5967 | 119.17 | 122.67 |
|  | aVTZ | 1.0110 | 107.37 | 122.35 | 1.5899 | 118.44 | 122.37 |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ (rot-planar) | aVDZ | 1.0163 | 109.18 | 125.41 | 1.5937 | 118.68 | 120.66 |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ (rot) | aVDZ | 1.4417 | 91.84 | 90.46 | 1.5933 | 119.77 | 1.8646 |
|  | aVTZ | 1.3971 | 91.71 | 90.02 | 1.5867 | 119.55 | 120.74 |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ (rot-planar) | aVDZ | 1.4073 | 109.18 | 125.41 | 1.5868 | 119.98 | 120.07 |

TABLE 3: Calculated Imaginary Vibrational MP2/ (cc-pVTZ) Frequencies ( $\mathrm{cm}^{-1}$ )

| molecule | symmetry | calcd | type |
| :--- | :---: | ---: | :--- |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}$ rot | $\mathrm{a}^{\prime \prime}$ | 778.9 i | rotation |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ rot | $\mathrm{a}^{\prime \prime}$ | 393.1 i | rotation |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ rot | $\mathrm{a}^{\prime \prime}$ | 516.2 i | rotation |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ rot | $\mathrm{a}^{\prime \prime}$ | 186.5 i | rotation |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}$ rot-planar | $\mathrm{a}_{2}$ | 1186.2 i | rotation |
|  | $\mathrm{b}_{2}$ | 631.5 i | inversion |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ rot-planar | $\mathrm{a}_{2}$ | 1150.7 i | rotation |
|  | $\mathrm{b}_{2}$ | 870.7 i | inversion |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ rot-planar | $\mathrm{a}_{2}$ | 549.3 i | rotation |
|  | $\mathrm{b}_{2}$ | 164.2 i | inversion |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ rot-planar | $\mathrm{b}_{2}$ | 641.8 i | inversion |
|  | $\mathrm{a}_{2}$ | 532.7 i | rotation |

is needed, but a correction of $0.03 \mathrm{kcal} / \mathrm{mol}$ is needed for B and one of $0.21 \mathrm{kcal} / \mathrm{mol}$ for Al , taken from the excitation energies of Moore. ${ }^{39}$

To calculate the zero point energy correction, we scaled the $\mathrm{M}-\mathrm{H}$ frequencies by the factors 0.96 for $\mathrm{M}=\mathrm{B}$ and $\mathrm{M}=\mathrm{N}$, 0.95 for $\mathrm{M}=\mathrm{P}$, and 0.954 for $\mathrm{M}=\mathrm{Al}$. These scale factors were obtained by taking the average of the $\operatorname{CCSD}(\mathrm{T}) /$ aug-ccpVTZ values and the experimental values for the $\mathrm{M}-\mathrm{H}$ stretches for the $\mathrm{MH}_{3}$ compounds and dividing them by the MP2/ccpVTZ value. Thus we estimate that the error introduced in the heats of formation due to the zero point energies is a maximum of $\pm 0.5 \mathrm{kcal} / \mathrm{mol}$.

By combining our computed $\Sigma D_{0}$ (total atomization energies) values with the known heats of formation at 0 K for the elements $\Delta H_{\mathrm{f}}{ }^{0}(\mathrm{~N})=112.53 \pm 0.02 \mathrm{kcal} \mathrm{mol}^{-1}, \Delta H_{\mathrm{f}}{ }^{0}(\mathrm{~B})=136.2 \pm 0.2$ $\mathrm{kcal} \mathrm{mol}{ }^{-1}, \Delta H_{\mathrm{f}}{ }^{0}(\mathrm{P})=75.42 \pm 0.24 \mathrm{kcal} \mathrm{mol}^{-1}, \Delta H_{\mathrm{f}}{ }^{0}(\mathrm{Al})=$ $78.23 \pm 1.0 \mathrm{kcal} \mathrm{mol}^{-1}$, and $\Delta H_{\mathrm{f}}{ }^{0}(\mathrm{H})=51.63 \mathrm{kcal} \mathrm{mol}^{-1},{ }^{40}$ we can derive $\Delta H_{\mathrm{f}}{ }^{0}$ values for the molecules under study in the gas phase. We obtain heats of formation at 298 K by following the procedures outlined by Curtiss et al. ${ }^{28}$

## Results and Discussion

The calculated geometries of the orthogonal transition state structures, corresponding to rotation about the AX bond, and the $C_{2 v}$ structures obtained by rotating about the $\mathrm{A}-\mathrm{X}$ bond and planarizing the $\mathrm{AH}_{2}$ and $\mathrm{XH}_{2}$ groups are given in Table 2. In addition, structures for planar $\mathrm{NH}_{3}$ and $\mathrm{PH}_{3}$ and the triatomic molecules $\mathrm{BH}_{2}, \mathrm{AlH}_{2}$, and $\mathrm{PH}_{2}$ are provided as Supporting Information. The calculated vibrational frequencies for all of the structures have been included in Supporting Information. For the rotated structures and the rotated-planar $C_{2 v}$ structures, the unique imaginary frequencies associated with each molecule, are given in Table 3. The $C_{s}$ structures are characterized by one imaginary frequency corresponding to rotation about the $\mathrm{A}-\mathrm{X}$ bond and the $C_{2 v}$ structures by two imaginary frequencies
with the second imaginary frequency corresponding to inversion at X . The molecular structures for the optimized ground states and the lowest energy transition states for rotation are shown in Figure 1.

The rotation process leads to breaking the $\pi$-bond and a consequent lengthening of the XY bond. The BN bond length of $\mathrm{BH}_{2} \mathrm{NH}_{2}$ increases by $0.084 \AA$ in going from the planar


Figure 1. Optimized molecular structures for $\mathrm{BH}_{2} \mathrm{NH}_{2}, \mathrm{AlH}_{2} \mathrm{NH}_{2}, \mathrm{BH}_{2}-$ $\mathrm{PH}_{2}, \mathrm{AlH}_{2} \mathrm{PH}_{2}$, and the corresponding rotated structures.

TABLE 4: Components for Calculated Atomization Energies ${ }^{a}$

| molecule | $\mathrm{CBS}^{b}$ | $\Delta E_{\mathrm{ZPE}^{c}}$ | $\Delta E_{\mathrm{CV}^{d}}$ | $\Delta E_{\mathrm{SR}^{e}}$ | $\Delta E_{\mathrm{So}}{ }^{f}$ |
| :--- | :---: | ---: | ---: | ---: | ---: | ---: |
| $\mathrm{BH}_{2}$ | 169.28 | 8.97 | 0.72 | -0.06 | -0.03 |
| $\mathrm{AlH}_{2}$ | 125.53 | 6.36 | -0.91 | -0.28 | -0.21 |
| $\mathrm{PH}_{2}$ | 154.32 | 8.32 | 0.19 | -0.22 | 0.00 |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}$ (rot) | 467.89 | 27.75 | 1.55 | -0.36 | -0.03 |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}$ (rot-planar) | 463.38 | 27.13 | 1.59 | -0.42 | -0.03 |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ (rot) | 406.37 | 22.67 | 1.28 | -0.43 | -0.03 |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ (rot-planar) | 373.49 | 22.20 | 0.97 | -0.79 | -0.03 |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ (rot) | 411.19 | 22.85 | -0.31 | -0.70 | -0.21 |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ (rot-planar) | 410.67 | 22.58 | -0.45 | -0.73 | 387.39 |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ (rot) | 351.94 | 18.36 | -0.59 | -0.69 | 351.44 |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ (rot-planar) | 330.91 | 18.10 | -0.99 | -1.04 | 387.12 |

${ }^{a}$ In $\mathrm{kcal} / \mathrm{mol} .{ }^{b}$ Extrapolated by using eq 1 with aug-cc-PVnZ, $n=\mathrm{D}, \mathrm{T}, \mathrm{Q} .{ }^{c}$ The zero point energies were obtained as described in the text. ${ }^{d}$ Core-valence corrections were obtained with the cc-pwCVTZ basis sets at the aVTZ optimized geometries for the transition states for rotation and at the aVDZ optimized geometries for the rotated-planar structures. ${ }^{e}$ The scalar relativistic correction is based on a CISD(FC)/cc-pVTZ MVD calculation at the aVTZ optimized geometries for the transition states for rotation and at the aVDZ optimized geometries for the rotated-planar structures. ${ }^{f}$ Correction due to the incorrect treatment of the atomic asymptotes as an average of spin multiplets. Values are based on C. Moore's Tables, ref $39 .{ }^{g}$ The theoretical value of the dissociation energy to atoms, $\Sigma D_{0}(0 \mathrm{~K})$.
ground-state configuration to the $90^{\circ}$-rotated $C_{s}$ symmetry transition state structure. For the rotated-planar $C_{2 v}$ structure of $\mathrm{BH}_{2} \mathrm{NH}_{2}$, the XY bond shows a smaller increase of 0.067 A . A similar increase was found for $\mathrm{BH}_{2} \mathrm{PH}_{2}$ with the BP bond lengthening of $0.082 \AA$ from the ground state to the rotated structure. There was a decrease in the XY bond distance of 0.017 $\AA$ going from the rotated to the planar-rotated $C_{2 v}$ structure. Upon rotation, a smaller increase of $0.040 \AA$ was found for the AlN bond of $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ from the planar ground state to the $C_{s}$ transition state structure. In going from the rotated $C_{s}$ structure to the planar-rotated $C_{2 v}$ structure, a similar decrease of 0.018 $\AA$ was predicted as was found for the other molecules. The AlP bond of $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ had a similar small increase of $0.027 \AA$ on rotation to the $C_{s}$ structure. In going from the rotated $C_{s}$ structure to the rotated-planar $C_{2 v}$ structures, there was a considerable decrease in the AIP bond distance of $0.070 \AA$. In comparison, Dobbs and Hehre ${ }^{9}$ calculated a much larger increase of $0.15 \AA$ in the $\mathrm{C}-\mathrm{C}$ bond length in going from the planar to the twisted form of ethylene at the UHF/6-31G* level. We note that the rotated form of $\mathrm{C}_{2} \mathrm{H}_{4}$ is a diradical as compared to the closed shell with a lone pair structure found in rotated $\mathrm{AH}_{2} \mathrm{XH}_{2}$.

The total valence $\operatorname{CCSD}(\mathrm{T})$ energies as a function of basis set are given in Supporting Information. The calculated energy components for the total atomization energies are given in Table 4 and the calculated heats of formation at 0 K and 298 K are given in Table 5. The previously reported results for the ground states are reported for completeness, and the results for planar $\left(C_{2 v}\right) \mathrm{BH}_{2} \mathrm{PH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ also are given in Table 5. ${ }^{3,4}$ The relativistic corrections for the structures investigated are all negative and reasonably small ranging from -0.06 to -1.04 $\mathrm{kcal} / \mathrm{mol}$. The core-valence corrections are positive for the $\mathrm{BH}_{2}$, $\mathrm{PH}_{2}, \mathrm{BH}_{2} \mathrm{NH}_{2}$, and $\mathrm{BH}_{2} \mathrm{PH}_{2}$ and range from 0.2 to $1.6 \mathrm{kcal} /$ mol. For $\mathrm{AlH}_{2}, \mathrm{AlH}_{2} \mathrm{NH}_{2}$, and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$, the core valence corrections are negative and range from -0.3 to $-1.0 \mathrm{kcal} /$ mol.

The $\pi$-bond energies can be estimated from the magnitude of the energies of the rotation barriers. There are three values for the rotation barrier given in Table 6. The adiabatic rotation energy barriers were calculated as the energy difference between the equilibrium ground-state configuration and the $C_{s}$ transition state for torsion about the $\mathrm{A}-\mathrm{X}$ bond. The values from the $C_{s}$ or $C_{2 v}$ ground state to the rotated $C_{2 v}$ structure were calculated as were the values for the rotation barrier from a $C_{2 v}$ planar structure to a $C_{2 v}$ rotated structure.

The adiabatic rotation barrier of borane amine is $29.9 \mathrm{kcal} /$ mol , which is much larger than found for the other molecules

TABLE 5: Calculated Heats of Formation (kcal/mol) at 0 K and 298 K

| molecule | $\Delta H_{\mathrm{f}}(0 \mathrm{~K})_{\text {theory }}$ | $\Delta H_{\mathrm{f}}(298 \mathrm{~K})_{\text {theory }}$ |
| :---: | :---: | :---: |
| $\mathrm{BH}_{2}$ | 78.5 | 78.6 |
| $\mathrm{AlH}_{2}$ | 63.7 | 63.0 |
| $\mathrm{PH}_{2}$ | 32.7 | 31.8 |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}$ (rot) | 14.0 | 11.1 |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}$ (rot-planar) | 17.9 | 15.0 |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ (rot) | 33.6 | 30.7 |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ (rot-planar) | 66.7 | 63.8 |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ (rot) | 10.2 | 7.1 |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ (rot-planar) | 10.6 | 7.2 |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ (rot) | 28.1 | 24.8 |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ (rot-planar) | 49.6 | 46.2 |
| $\mathrm{BH}_{2} \mathrm{NH}_{2}\left(\mathrm{GS} \mathrm{C} C_{2 v}\right)^{a}$ | -15.9 | -18.6 |
| $\mathrm{AlH}_{2} \mathrm{NH}_{2}(\mathrm{GS} \mathrm{C} \mathrm{C} 2 v)^{b}$ | -0.3 | -3.3 |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}\left(\mathrm{GS} C_{s}\right)^{b}$ | 24.4 | 21.8 |
| $\mathrm{BH}_{2} \mathrm{PH}_{2}$ (planar $\left.C_{2 v}\right)^{\text {b }}$ | 31.0 | 28.2 |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}\left(\mathrm{GS} \mathrm{C} C_{5}\right)^{b}$ | 25.4 | 22.6 |
| $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ (planar $\left.C_{2 v}\right)^{\text {b }}$ | 35.4 | 32.2 |

${ }^{a} \operatorname{Ref} 3 .{ }^{b} \operatorname{Ref} 4$.
and indicative of a strong dative $\pi$-bond between B and N . This value is much lower than the $\pi$-bond strength of $65 \mathrm{kcal} / \mathrm{mol}^{-1}$ in ethylene ${ }^{11}$ obtained from the rate of cis-trans isomerization in 1,2-dideuterioethylene. Our value for $\mathrm{BH}_{2} \mathrm{NH}_{2}$ is in good agreement with that of Allen and Fink, ${ }^{12}$ who predicted a rotational barrier ( $C_{\mathrm{s}}$ symmetry transition state) of $32.4 \mathrm{kcal} /$ mol at the CISD $+\mathrm{Q} / \mathrm{DZ}+\mathrm{P}$ level and of McKee ${ }^{14}$ who predicted $32.1 \mathrm{kcal} / \mathrm{mol}$ at the MP4/6-31+G(2d,p) level of theory.

The adiabatic dative $\pi$-bond energy of $\mathrm{H}_{2} \mathrm{AlNH}_{2}$ is about onethird that of borane amine, $10.5 \mathrm{kcal} / \mathrm{mol}$, consistent with the smaller change in bond distance on rotation and the lower $\pi$-bond energy expected for a bond between a 1 st and 2 nd row metal. The lower level values calculated by Fink ${ }^{19}$ and Davy ${ }^{20}$ of 11.2 and $11.0 \mathrm{kcal} / \mathrm{mol}$, respectively, are in excellent agreement with our higher level calculation. Borylphosphine, $\mathrm{H}_{2} \mathrm{BPH}_{2}$, has a similar adiabatic $\pi$-bond energy of $9.2 \mathrm{kcal} /$ mol. Surprisingly, the $\mathrm{B}-\mathrm{P}$ bond distance increases by an amount comparable to that of $\mathrm{BH}_{2} \mathrm{NH}_{2}$ on rotation even though the latter has a much higher barrier. Borden ${ }^{18}$ calculated the adiabatic barrier to rotation in $\mathrm{BH}_{2} \mathrm{PH}_{2}$ to be $10.4 \mathrm{kcal} / \mathrm{mol}$ at the MP4 level of theory, which is in good agreement with our value. Allen et al. ${ }^{16}$ also calculated the rotational barrier in $\mathrm{BH}_{2}-$ $\mathrm{PH}_{2}$ through a transition state of $C_{s}$ symmetry at $10.0 \mathrm{kcal} /$ mol. The rotational energy barrier for the phosphine alane was considerably smaller than the others indicating a very weak adiabatic $\pi$-bond between AlP. The adiabatic $\pi$-bond energy

TABLE 6: Rotation Barriers ( $\boldsymbol{\pi}$-Bond Energies) and Inversion Barriers at $\mathbf{N}$ or $\mathbf{P}^{a}$

| molecule | rotation $\left(G . S \rightarrow C_{s}\right)$ <br> adiabatic ${ }^{b}$ | rotation <br> $\left(C_{s} \rightarrow C_{2 v}\right)$ | rotation $\left(C_{2 v} \rightarrow C_{2 v}\right)$ <br> inherent ${ }^{c}$ | inversion <br> (ground state) | inversion <br> (rotated) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{~B}=\mathrm{NH}_{2}$ | 29.9 | 33.8 | 33.8 | $0^{d}$ | 3.9 |
| $\mathrm{H}_{2} \mathrm{Al}=\mathrm{NH}_{2}$ | 10.5 | 10.9 | 10.9 | $0^{d}$ | 6.4 |
| $\mathrm{H}_{2} \mathrm{~B}=\mathrm{PH}_{2}$ | 9.2 | 42.3 | 35.7 | 3.4 |  |
| $\mathrm{H}_{2} \mathrm{Al}=\mathrm{PH}_{2}$ | 2.7 | 24.2 | 14.2 | 10.0 | 21.5 |

${ }^{a}$ In kcal/mol. ${ }^{b}$ Adiabtic $\pi$-bond energy. ${ }^{c}$ Intrinsic $\pi$-bond energy. ${ }^{d}$ Planar ground-state structure.


Figure 2. HOMO for the ground state and rotated structures of $\mathrm{BH}_{2}-$ $\mathrm{NH}_{2}, \mathrm{AlH}_{2} \mathrm{NH}_{2}, \mathrm{BH}_{2} \mathrm{PH}_{2}$, and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$.
of $\mathrm{H}_{2} \mathrm{AlPH}_{2}$ was about one-third that of borane phosphine's at $2.7 \mathrm{kcal} / \mathrm{mol}$.

We provide plots of the highest occupied molecular orbital (HOMO) at the Hartree-Fock level for the ground state and the transition state for rotation in Figure 2. The HOMO in the planar structures corresponds essentially to a lone pair on N or P that can delocalize to the B or Al . The largest delocalization is found for $\mathrm{BH}_{2} \mathrm{NH}_{2}$ as expected from this compound having the highest barrier. The other molecules, which have much lower rotation barriers, show less delocalization from the lone pair on X toward the empty orbital on A with the smallest change in the orbitals found for $\mathrm{AlH}_{2} \mathrm{PH}_{2}$, the compound with the lowest barrier. There is a small interaction of the lone pair on N with the $\mathrm{A}-\mathrm{H}$ orbitals in the rotated transition state. The orbital plots confirm that the $\pi$-bond in these $\mathrm{AH}_{2} \mathrm{XH}_{2}$ compounds is best described as a dative bond just as found for the $\sigma$-bond in the $\mathrm{AH}_{3} \mathrm{XH}_{3}$ compounds.

We also calculated a rotation barrier as the energy difference between the ground state and the rotated-planar $C_{2 v}$ structures.

This information can be used to provide insights into the heights of the barriers. The rotation barrier for $\mathrm{BH}_{2} \mathrm{NH}_{2}$ is $33.8 \mathrm{kcal} /$ mol going from the $C_{2 v}$ ground state to the rotated $C_{2 v}$ structure, similar to the value of $37.9 \mathrm{kcal} / \mathrm{mol}$ of Allen and Fink. ${ }^{12} \mathrm{~A}$ much smaller value of $10.9 \mathrm{kcal} / \mathrm{mol}$ was obtained for the $C_{2 v^{-}}$ $C_{2 v}$ rotational barrier in $\mathrm{AlH}_{2} \mathrm{NH}_{2}$. The barrier to rotation in going from the ground-state nonplanar $\mathrm{BH}_{2} \mathrm{PH}_{2} \mathrm{C}_{\mathrm{s}}$ structure to the rotated $C_{2 v}$ structure is $42.3 \mathrm{kcal} / \mathrm{mol}$, similar to the values obtained by Borden ${ }^{18}$ of $44.6 \mathrm{kcal} / \mathrm{mol}$ and by Allen and Fink ${ }^{16}$ of $46.4 \mathrm{kcal} / \mathrm{mol}$. In $\mathrm{AlH}_{2} \mathrm{PH}_{2}$, the $C_{s}-C_{2 v}$ rotation barrier is 24.2 $\mathrm{kcal} / \mathrm{mol}$. The final rotation barrier to be considered is the barrier to rotation between the planar $C_{2 v}$ structure and the rotatedplanar $C_{2 v}$ structure for $\mathrm{BH}_{2} \mathrm{PH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ with respective values of 35.7 and $14.2 \mathrm{kcal} /$ mole.

To better understand the rotation energies, we need to consider the inversion barriers at N and P . The molecular structures of most $\mathrm{BY}_{3}$ and $\mathrm{AlY}_{3}$ compounds are planar so inversion does not occur at them. We calculate a barrier height for the inversion of ammonia of $5.1 \mathrm{kcal} / \mathrm{mol}$ at the $\operatorname{CCSD}(\mathrm{T})$ / CBS limit, about $0.7 \mathrm{kcal} / \mathrm{mol}$ below the experimental ${ }^{13}$ barrier height of $2020 \pm 12 \mathrm{~cm}^{-1}(5.77 \mathrm{kcal} / \mathrm{mol})$. Including the zeropoint contribution, we obtain a value of $5.0 \mathrm{kcal} / \mathrm{mol}$ for the inversion of $\mathrm{NH}_{3}$. We calculate the inversion barrier of $\mathrm{PH}_{3}$ to be $33.6 \mathrm{kcal} / \mathrm{mol}$ that decreases to $32.9 \mathrm{kcal} / \mathrm{mol}$ with the zeropoint correction included. This value is similar to that of Marynick and Dixon ${ }^{17}$ who calculated a barrier for $\mathrm{PH}_{3}$ of 34.4 $\mathrm{kcal} / \mathrm{mol}$ at the SCF-CI/DZ+P level including an estimate for quadruple excitations.

We calculated the inversion of the nonplanar $-\mathrm{PH}_{2}$ moiety in the ground-state structures of $\mathrm{BH}_{2} \mathrm{PH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ to be 6.6 and $10.0 \mathrm{kcal} / \mathrm{mol}$, respectively, with both considerably less than the inversion barrier of $\mathrm{PH}_{3}$. This is consistent with the fact that the $\mathrm{BH}_{2}$ and $\mathrm{AlH}_{2}$ groups are electropositive, which is known to decrease the inversion barrier. In addition, the presence of the dative $\pi$-bond can lower the inversion barrier. Borden ${ }^{18}$ finds a smaller barrier to planarity in $\mathrm{BH}_{2} \mathrm{PH}_{2}$ of $4.5 \mathrm{kcal} / \mathrm{mol}$ at the MP4/6-31G* level.

The barriers to inversion of the $-\mathrm{NH}_{2}$ and $-\mathrm{PH}_{2}$ moieties in the rotated structures at the $\operatorname{CCSD}(\mathrm{T}) / \mathrm{CBS}$ level also were calculated. This provides an estimate of the electropositive effect as no $\pi$-bond is present. For $\mathrm{BH}_{2} \mathrm{NH}_{2}$, the barrier to invert $\mathrm{NH}_{2}$ in the rotated structure is $3.9 \mathrm{kcal} / \mathrm{mol}$, slightly lower than our calculated value of $5.0 \mathrm{kcal} / \mathrm{mol}$ for the inversion barrier of $\mathrm{NH}_{3}$, showing a small effect of substitution of $\mathrm{BH}_{2}$ for H when there is no overlap of the lone pair on N with the vacant orbital on B. For rotated $\mathrm{AlH}_{2} \mathrm{NH}_{2}$, the barrier to inversion was $0.4 \mathrm{kcal} /$ mol considerably less than that in $\mathrm{BH}_{2} \mathrm{NH}_{2}$, and consistent with the fact that $\mathrm{AlH}_{2}$ is more electropositive than $\mathrm{BH}_{2}$. For rotated $\mathrm{BH}_{2} \mathrm{PH}_{2}$, the barrier to inversion of the $-\mathrm{PH}_{2}$ moiety was 33.1 $\mathrm{kcal} / \mathrm{mol}$ showing essentially no effect of substituting $\mathrm{BH}_{2}$ for H , just as was found for the nitrogen analogue. For rotated $\mathrm{AlH}_{2}{ }^{-}$ $\mathrm{PH}_{2}$, the barrier to inversion was $21.5 \mathrm{kcal} / \mathrm{mol}$, considerably less than that in $\mathrm{BH}_{2} \mathrm{PH}_{2}$. The decrease of $11.4 \mathrm{kcal} / \mathrm{mol}$ on substitution of $\mathrm{AlH}_{2}$ for H is again consistent with $\mathrm{AlH}_{2}$ being more electropositive than $\mathrm{BH}_{2}$ or H .

## TABLE 7: Adiabatic $(\sigma+\pi)$ Total Dissociation Energies ${ }^{a}$

| molecule | adiabatic total <br> dissociation energy | adiabatic <br> $\sigma$-bond energy |
| :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{~B}=\mathrm{NH}_{2}$ | 139.7 | 109.8 |
| $\mathrm{H}_{2} \mathrm{Al}=\mathrm{NH}_{2}$ | 109.3 | 98.8 |
| $\mathrm{H}_{2} \mathrm{~B}=\mathrm{PH}_{2}$ | 86.8 | 77.6 |
| $\mathrm{H}_{2} \mathrm{Al}=\mathrm{PH}_{2}$ | 71.0 | 68.3 |
| ${ }^{a}$ In $\mathrm{kcal} / \mathrm{mol}$. |  |  |

On the basis of these values, we can now reexamine the $\pi$-bond strengths. For $\mathrm{BH}_{2} \mathrm{NH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{NH}_{2}$, the differences between the rotation barrier proceeding through the rotated $C_{s}$ and $C_{2 v}$ structures are similar due to the relatively small inversion barrier at N . For $\mathrm{BH}_{2} \mathrm{PH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$, the difference between the rotation barrier proceeding through the rotated $C_{s}$ and $C_{2 v}$ structures is due to the much larger inversion barrier at $P$. The tendency for the phosphorus atom to pyramidalize serves to weaken the $\pi$-bond energy because there is reduced overlap between the lone pair on P and the vacant orbital at B or Al . We can estimate this effect by comparing the inversion barriers in the unrotated and rotated states which corresponds to the $C_{2 v^{-}}$ $C_{2 v}$ energy difference. For $\mathrm{BH}_{2} \mathrm{PH}_{2}$, this value is $35.7 \mathrm{kcal} / \mathrm{mol}$ and, in $\mathrm{AlH}_{2} \mathrm{PH}_{2}$, this value is $14.2 \mathrm{kcal} / \mathrm{mol}$.

The adiabatic $\pi$-bond energies are the ground state (GS) to $C_{s}$ values given in Table 6 . The intrinsic $\pi$-bond energies are given by the adiabatic bond energy plus the energy used to invert the N or P atom or the $C_{2 v} \rightarrow C_{2 v}$ rotation energies. The intrinsic $\mathrm{B}=\mathrm{N} \pi$-bond energy is thus $34 \mathrm{kcal} / \mathrm{mol}$ and the intrinsic $\mathrm{Al}=$ $\mathrm{N} \pi$-bond energy is $11 \mathrm{kcal} / \mathrm{mol}$, both similar to the adiabatic values. The intrinsic $\mathrm{B}=\mathrm{P} \pi$-bond energy is $36 \mathrm{kcal} / \mathrm{mol}$ and the intrinsic $\mathrm{Al}=\mathrm{P} \pi$-bond energy is $14 \mathrm{kcal} / \mathrm{mol}$. The intrinsic $\pi$-bond energies for the latter two are substantially different from the adiabatic values because of the high inversion barrier at P . Comparing the intrinsic values, we see that the $B=N$ and $B=P$ values are quite similar and that the $\mathrm{Al}=\mathrm{N}$ and $\mathrm{Al}=\mathrm{P}$ values also are similar and substantially smaller.

On the basis of the calculated heats of formations given in Table 5, the adiabatic dissociation energies which correspond to the sum of the $\sigma$ - and $\pi$-bond energies are given in Table 7 . The adiabatic reaction energies show that $\mathrm{BH}_{2} \mathrm{NH}_{2}$ has the largest binding energy at $139.7 \mathrm{kcal} / \mathrm{mol}$, which can be compared with the $\mathrm{C}-\mathrm{C}$ bond dissociation energy of $171.0 \mathrm{kcal} / \mathrm{mol}$ in ethylene. ${ }^{6} \mathrm{AlH}_{2} \mathrm{NH}_{2}$ has a binding energy approximately $20 \mathrm{kcal} /$ mol lower than that of $\mathrm{BH}_{2} \mathrm{NH}_{2}(109.3 \mathrm{kcal} / \mathrm{mol})$. Both the $\mathrm{BH}_{2}-$ $\mathrm{PH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ have lower binding energies of 86.8 and 71.0 $\mathrm{kcal} / \mathrm{mol}$, respectively.

The adiabatic $\sigma$-bond energies of the molecules can be calculated as the difference between the binding energy of the optimized ground-state structure, representing the $\sigma$-bond + $\pi$-bond energies, and the corresponding adiabatic rotational energy barrier, representing the $\pi$-bond energy. The adiabatic $\sigma$-bond strengths for the molecules $\mathrm{BH}_{2} \mathrm{NH}_{2}, \mathrm{AlH}_{2} \mathrm{NH}_{2}, \mathrm{BH}_{2}-$ $\mathrm{PH}_{2}$, and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ from the $(\sigma+\pi)$ adiabatic asymptote using the adiabatic rotation barriers are 109.8, 98.8, 77.6, and 68.3 $\mathrm{kcal} / \mathrm{mol}$, respectively. The adiabatic $\sigma$-bond strength for $\mathrm{BH}_{2}-$ $\mathrm{NH}_{2}$ is comparable to the adiabatic $\sigma$-bond strength in ethylene of $106 \mathrm{kcal} / \mathrm{mol}$ given the experimentally determined $\pi$-bond strength of $65 \mathrm{kcal} / \mathrm{mol}^{11}$ and an adiabatic $\mathrm{C}=\mathrm{C}$ bond dissociation energy of $171 \mathrm{kcal} / \mathrm{mol} .{ }^{5}$ The fact that it is slightly higher is consistent with the fact that the bond in $\mathrm{BH}_{2} \mathrm{NH}_{2}$ includes some ionic character. If we use the intrinsic $\pi$-bond strengths, we lower the adiabatic $\sigma$-bond strength to $106 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{BH}_{2}-$ $\mathrm{NH}_{2}$. For $\mathrm{AlH}_{2} \mathrm{NH}_{2}$, use of the intrinsic $\pi$-bond strength results in very little change, a $\sigma$-bond strength of $98 \mathrm{kcal} / \mathrm{mol}$. For $\mathrm{BH}_{2}-$ $\mathrm{PH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$, use of the intrinsic $\pi$-bond strengths leads
to substantially lower $\sigma$-bond strengths of 51.1 and $56.8 \mathrm{kcal} /$ mol, respectively.

The adiabatic $\sigma$-bond energies can be compared to the bond dissociation energies of the diatomics BN, AlN, BP, and AlP that are $102.4,57.3,76.4$, and $50.9 \mathrm{kcal} / \mathrm{mol}$ at 0 K , respectively. ${ }^{3,4}$ Thus the $\sigma$-bond energies are stronger in the molecular systems than in the diatomics. In contrast, the dissociation energy ${ }^{41}$ of $C_{2}$ is $148 \mathrm{kcal} / \mathrm{mol}$, much higher than the $\mathrm{C}-\mathrm{C}$ $\sigma$-bond energies in most organic compounds.

The $\sigma$-bond energies for the $\mathrm{AH}_{2} \mathrm{XH}_{2}$ compounds can be compared to the dative $\sigma$-bond energies in the corresponding $\mathrm{AH}_{3} \mathrm{XH}_{3}$ compound (Table 1). The $\sigma$-bond energies for the $\mathrm{AH}_{2}-$ $\mathrm{XH}_{2}$ compounds are substantially higher than the dative $\sigma$-bond energies. As a consequence, the reaction $\mathrm{AH}_{3} \mathrm{XH}_{3} \rightarrow \mathrm{AH}_{2} \mathrm{XH}_{2}$ $+\mathrm{H}_{2}$ becomes closer to thermoneutral than in the hydrocarbon case for $\mathrm{CH}_{3} \mathrm{CH}_{3} \rightarrow \mathrm{CH}_{2} \mathrm{CH}_{2}+\mathrm{H}_{2}$, which is substantially endothermic. Only for the $\mathrm{BH}_{3} \mathrm{PH}_{3}$ reaction is a substantial endothermicity found, and this is consistent with the relatively low $\sigma$-bond energy.

Carter and Goddard ${ }^{8}$ have shown that most of the decrease in the dissociation energy of $\mathrm{C}_{2} \mathrm{~F}_{4}$ to $2 \mathrm{CF}_{2}$ as compared to the dissociation energy of $\mathrm{C}_{2} \mathrm{H}_{4}$ to $2 \mathrm{CH}_{2}$ is due to the difference in the ground states of $\mathrm{CF}_{2}$ and $\mathrm{CH}_{2}$. The singlet ground state of $\mathrm{CF}_{2}$ is not optimal for forming the $\sigma$ - and $\pi$-bonds in $\mathrm{C}_{2} \mathrm{~F}_{4}$, so the total dissociation energy is substantially reduced by the promotion energy to the triplet configuration, which is optimal for forming $\mathrm{C}_{2} \mathrm{~F}_{4}$. In $\mathrm{C}_{2} \mathrm{H}_{4}$, the triplet ground state of $\mathrm{CH}_{2}$ is optimal for forming $\mathrm{C}_{2} \mathrm{H}_{4}$, so there is no reduction in the total bond dissociation energy. Borden ${ }^{7}$ has suggested that the same types of arguments need to be considered in comparing the strengths of the $\pi$-bonds in $\mathrm{C}_{2} \mathrm{H}_{4}$ and HCCH . This is because the optimal state of CH for forming HCCH is the ${ }^{4} \Sigma^{-}$, which is $16.7 \mathrm{kcal} / \mathrm{mol}$ above the ${ }^{2} \Pi$ ground state.

This approach can be applied to analyze the bonding of $\mathrm{AH}_{2}{ }^{-}$ $\mathrm{XH}_{2}$ compounds to derive an intrinsic total $(\sigma+\pi)$ bond dissociation energy. The bonding in the molecules at equilibrium corresponds to $\mathrm{BH}_{2}$ or $\mathrm{AlH}_{2}$ in the ground state and the $\mathrm{NH}_{2}$ or $\mathrm{PH}_{2}$ in the excited state. The excited state for $\mathrm{XH}_{2}$ is the ${ }^{2} \mathrm{~A}_{1}$ with the unpaired electron in the plane and the lone pair orbital out of the plane. For $\mathrm{NH}_{2}, \mathrm{~T}_{0}\left({ }^{2} \mathrm{~B}_{1} \rightarrow{ }^{2} \mathrm{~A}_{1}\right)$ is $31.8 \mathrm{kcal} / \mathrm{mol}$ and for $\mathrm{PH}_{2}, \mathrm{~T}_{0}$ is $52.2 \mathrm{kcal} / \mathrm{mol} .^{42}$ To a first approximation, the bonding in $\mathrm{H}_{2} \mathrm{~A}=\mathrm{XH}_{2}$ can be described as arising from the ${ }^{2} \mathrm{~A}_{1}$ configurations of both fragments. Thus, the sum of the bond energies in the diabatic limit or the intrinsic total $(\sigma+\pi)$ bond dissociation energy would be increased by $31.8 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{BH}_{2} \mathrm{NH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ and by $52.2 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{BH}_{2} \mathrm{PH}_{2}$ and $\mathrm{AlH}_{2} \mathrm{PH}_{2}$ giving respective values of $171.5,141.1,139.0$, and $123.2 \mathrm{kcal} / \mathrm{mol}$. If the intrinsic total $(\sigma+\pi)$ bond dissociation energy is used, then $\mathrm{BH}_{2} \mathrm{NH}_{2}$ has a $\sigma$-bond strength of $142 \mathrm{kcal} /$ mol using the adiabatic rotation barrier and one of $138 \mathrm{kcal} /$ mol using the intrinsic $\pi$-bond energy. For $\mathrm{AlH}_{2} \mathrm{NH}_{2}$, the $\sigma$-bond strengths are 131 and $130 \mathrm{kcal} / \mathrm{mol}$, respectively, using the two definitions of the $\pi$-bond energy. For $\mathrm{BH}_{2} \mathrm{PH}_{2}$, the $\sigma$-bond energies would be $130 \mathrm{kcal} / \mathrm{mol}$ with the adiabatic $\pi$-bond energy and $103 \mathrm{kcal} / \mathrm{mol}$ with the intrinsic the $\pi$-bond energy. For $\mathrm{AlH}_{2} \mathrm{PH}_{2}$, the $\sigma$-bond energies would be $121 \mathrm{kcal} / \mathrm{mol}$ with the adiabatic $\pi$-bond energy and $109 \mathrm{kcal} / \mathrm{mol}$ with the intrinsic $\pi$-bond energy. These values seem to be somewhat high and are not consistent with other chemical concepts.

This analysis suggested another way to analyze the bonding in these molecules. Because the $\pi$-bond is best described as a dative bond (see Figure 2), it is appropriate to compare breaking the $\sigma$-bond in these compounds to breaking an $\mathrm{AH}_{2}-\mathrm{R}$ or $\mathrm{XH}_{2}-\mathrm{R}$ bond. The simplest comparison is to consider R as H
and compare the $\mathrm{A}-\mathrm{H}$ and $\mathrm{X}-\mathrm{H}$ bond energies to the $\mathrm{A}-\mathrm{X}$ bond energies. Feller et al. ${ }^{43}$ calculated the heats of formation of some simple boron compounds and predicted $\Delta H_{\mathrm{f}}{ }^{0}\left(\mathrm{BH}_{2}, 0\right.$ $\mathrm{K})=78.4 \mathrm{kcal} / \mathrm{mol}$ and $\Delta H_{\mathrm{f}}{ }^{0}(\mathrm{BH}, 0 \mathrm{~K})=106.2 \mathrm{kcal} / \mathrm{mol}$ at the $\operatorname{CCSD}(\mathrm{T}) / \mathrm{CBS}$ level. These values for $\mathrm{BH}_{2}$ and BH are in good agreement with our current value of 78.5 and $106.2 \mathrm{kcal} /$ mol, respectively, where we have included scalar-relativistic and spin-orbit corrections, which were not included previously. Given the heat of formation of $\mathrm{BH}_{3}$ of $26.4 \mathrm{kcal} / \mathrm{mol}$ at $0 \mathrm{~K},{ }^{3}$ we calculate a B-H bond energy of $103.7 \mathrm{kcal} / \mathrm{mol}$ (see Table 8). In the present study, we have calculated the heats for formation at 0 K of the triatomics $\mathrm{AlH}_{2}$ and $\mathrm{PH}_{2}$, giving values of 63.7 and $32.7 \mathrm{kcal} / \mathrm{mol}$, respectively, and the corresponding diatomics AlH and PH, giving values of 58.9 and $57.0 \mathrm{kcal} /$ mol , respectively. Given $\Delta H_{f}{ }^{0}\left(\mathrm{AlH}_{3}, 0 \mathrm{~K}\right)=31.9 \mathrm{kcal} / \mathrm{mol}$ and $\Delta H_{\mathrm{f}}{ }^{0}\left(\mathrm{PH}_{3}, 0 \mathrm{~K}\right)=3.3 \mathrm{kcal} / \mathrm{mol},{ }^{4}$ the resulting $\mathrm{Al}-\mathrm{H}$ bond energy in $\mathrm{AlH}_{3}$ is $83.4 \mathrm{kcal} / \mathrm{mol}$, while the $\mathrm{P}-\mathrm{H}$ bond energy in $\mathrm{PH}_{3}$ is $81.0 \mathrm{kcal} / \mathrm{mol}$. These can be compared to the $\mathrm{B}-\mathrm{H}$ bond energy of $103.7 \mathrm{kcal} / \mathrm{mol}$ in $\mathrm{BH}_{3}$ and the $\mathrm{N}-\mathrm{H}$ bond energy of $106.5 \mathrm{kcal} / \mathrm{mol}$ in $\mathrm{NH}_{3}{ }^{3}$. The bond energies for $\mathrm{HAl}-\mathrm{H}$ and $\mathrm{HP}-\mathrm{H}$ in going to the corresponding diatomic species are $46.8 \mathrm{kcal} / \mathrm{mol}$ at 0 K and $75.9 \mathrm{kcal} / \mathrm{mol}$ at 0 K , respectively, and can be compared to the value of the $\mathrm{H}-\mathrm{BH}$ bond energy of $79.3 \mathrm{kcal} / \mathrm{mol}$ and the $\mathrm{H}-\mathrm{NH}$ bond energy of $92.3 \mathrm{kcal} / \mathrm{mol}$ at $0 \mathrm{~K} .{ }^{21 \mathrm{~m}}$

Comparison of the $\mathrm{AH}_{3}$ and $\mathrm{XH}_{3}$ bond energies in Table 8 with the $\mathrm{A}-\mathrm{B}$ adiabatic $\sigma$-bond energies in Table 7 shows that the $\mathrm{X}-\mathrm{H}$ bond energies track the $\mathrm{A}-\mathrm{B}$ bond energies. The $\sigma$-bond energy in $\mathrm{BH}_{2} \mathrm{NH}_{2}$ is larger than the $\mathrm{N}-\mathrm{H}$ bond energy in $\mathrm{NH}_{3}$ by only $3 \mathrm{kcal} / \mathrm{mol}$. The $\sigma$-bond energy in $\mathrm{AlH}_{2} \mathrm{NH}_{2}$ is less than that in $\mathrm{BH}_{2} \mathrm{NH}_{2}$ by $11 \mathrm{kcal} / \mathrm{mol}$ as is expected as Al is a 2 nd row atom and the bond energy is only $8 \mathrm{kcal} / \mathrm{mol}$ less than the $\mathrm{N}-\mathrm{H}$ bond energy in $\mathrm{NH}_{3}$. For $\mathrm{BH}_{2}=\mathrm{PH}_{2}$ and $\mathrm{AlH}_{2}=$ $\mathrm{PH}_{2}$, the $\sigma$-bond energies are 3 and $13 \mathrm{kcal} / \mathrm{mol}$, respectively, less than the $\mathrm{P}-\mathrm{H}$ bond energy in $\mathrm{PH}_{3}$, which is essentially the same trend found in comparing the $\sigma$-bond energies in $\mathrm{BH}_{2}=$ $\mathrm{NH}_{2}$ and $\mathrm{AlH}_{2}=\mathrm{NH}_{2}$ with the $\mathrm{N}-\mathrm{H}$ bond energy in $\mathrm{NH}_{3}$. Thus, the $\sigma$-bond energies resemble very closely the $\mathrm{XH}_{3}$ bond energies, and it is not appropriate to compare with the diabatic limit approximation given above. The bonding in these compounds is much closer to that in a normal $\mathrm{NH}_{2} \mathrm{R}$ or $\mathrm{PH}_{2} \mathrm{R}$ compound with a delocalized lone pair (dative $\pi$-bond) from N or P as compared to a model that describes the bonding as a fully shared $\pi$-bond as found in $\mathrm{C}_{2} \mathrm{H}_{4}$. This result is consistent with Pauling's electroneutrality rule ${ }^{44}$ as one would have to write the structure of $\mathrm{BH}_{2} \mathrm{NH}_{2}$ as ${ }^{-} \mathrm{H}_{2} \mathrm{~B}=\mathrm{NH}_{2}{ }^{+}$with formal charges that puts the negative charge on the least electronegative atom B and the positive charge on the more electronegative atom N , which is the reverse of where the charges want to be.

The bond energies for the $\mathrm{H}_{2} \mathrm{AXH}_{2}$ compounds provide us with some useful insights into the differences in the donoracceptor chemistry and covalent bond carbon-based chemistry. The elimination reaction 4 for loss of $\mathrm{H}_{2}$ from $\mathrm{BH}_{3} \mathrm{NH}_{3}$ in the gas phase is exothermic

$$
\begin{align*}
& \mathrm{BH}_{3} \mathrm{NH}_{3} \rightarrow \mathrm{BH}_{2} \mathrm{NH}_{2}+\mathrm{H}_{2} \\
& \Delta H(298 \mathrm{~K})=-5.1 \mathrm{kcal} / \mathrm{mol} \tag{4}
\end{align*}
$$

whereas the comparable organic reaction 5 is substantially endothermic. ${ }^{3}$

$$
\begin{equation*}
\mathrm{C}_{2} \mathrm{H}_{6} \rightarrow \mathrm{C}_{2} \mathrm{H}_{4}+\mathrm{H}_{2} \quad \Delta H(298 \mathrm{~K})=32.6 \mathrm{kcal} / \mathrm{mol} \tag{5}
\end{equation*}
$$

This difference in energetic requirements for $\mathrm{H}_{2}$ release is because a weak $\mathrm{B}-\mathrm{N}$ dative $\sigma$-bond is broken in $\mathrm{BH}_{3} \mathrm{NH}_{3}$ and

TABLE 8: $\mathbf{A H}_{2}-\mathrm{H}$ and $\mathbf{X H}_{2}-\mathrm{H} \boldsymbol{\sigma}$ Bond Energies ${ }^{a}$

| molecule | adiabatic $\sigma$-bond energy |
| :---: | :---: |
| $\mathrm{BH}_{3}$ | 103.7 |
| $\mathrm{NH}_{3}$ | 106.5 |
| $\mathrm{AlH}_{3}$ | 83.4 |
| $\mathrm{PH}_{3}$ | 81.0 |
| $a$ In kcal/mol. |  |

a strong $\mathrm{sp}^{2}-\mathrm{sp}^{2} \sigma$-bond is formed in $\mathrm{BH}_{2} \mathrm{NH}_{2}$, whereas a strong $\sigma$-bond is broken in $\mathrm{C}_{2} \mathrm{H}_{6}$ and a $\sigma$-bond of comparable strength to that in $\mathrm{BH}_{2} \mathrm{NH}_{2}$ is formed in $\mathrm{C}_{2} \mathrm{H}_{4}$. Even though the adiabatic $\pi$-bond energy of $\mathrm{BH}_{2} \mathrm{NH}_{2}$ is only $30 \mathrm{kcal} / \mathrm{mol}$ as compared to the value of $65 \mathrm{kcal} / \mathrm{mol}$ in $\mathrm{C}_{2} \mathrm{H}_{4}$, the difference of $35 \mathrm{kcal} / \mathrm{mol}$ is much smaller than the difference of $63 \mathrm{kcal} / \mathrm{mol}$ for the $\sigma$-bond strengths in $\mathrm{BH}_{3} \mathrm{NH}_{3}$ and $\mathrm{C}_{2} \mathrm{H}_{6}$. Thus, the difference in the reactant $\sigma$-bond strengths is more important than the differences in the product $\pi$-bond strengths, because the strength of the $\sigma$-bonds in the product are comparable. The differences in the $\sigma$ - and $\pi$-bond strengths also can be observed in the bond distances. The change in the $\mathrm{C}-\mathrm{C}$ bond length ${ }^{45}$ from $\mathrm{C}_{2} \mathrm{H}_{6}$ to $\mathrm{C}_{2} \mathrm{H}_{4}$ is $0.20 \AA$, whereas the difference in the $\mathrm{B}-\mathrm{N}$ bond lengths between $\mathrm{BH}_{3} \mathrm{NH}_{3}$ and $\mathrm{BH}_{2} \mathrm{NH}_{2}$ is $0.26 \AA$. The larger difference in the latter pair is consistent with the larger change in the $\sigma$-bond strengths in the boron amines, even though the $\pi$-bond strength is lower in the boron amines. The $\pi$-bond shortens the $\mathrm{B}-\mathrm{N}$ bond length by $0.08 \AA$ obtained by comparing the ground state and rotated structures for $\mathrm{BH}_{2} \mathrm{NH}_{2}$. In $\mathrm{C}_{2} \mathrm{H}_{4}$, the difference has been calculated ${ }^{9}$ to be $0.15 \AA$ at the UHF/6-31G* level $\left(\mathrm{C}_{2} \mathrm{H}_{4}\right.$ vs twisted $\left.\cdot \mathrm{CH}_{2} \mathrm{CH}_{2} \cdot\right)$, a larger difference consistent with the stronger $\pi$-bond in $\mathrm{C}_{2} \mathrm{H}_{4}$. The value of $1.465 \AA$ for the diradical $\mathrm{sp}^{2}-\mathrm{sp}^{2} \sigma$-bond is consistent with the experimental ${ }^{46}$ and calculated ${ }^{47}$ values of 1.45 to $1.47 \AA$ for the $\mathrm{C}-\mathrm{C} \mathrm{sp}^{2}-$ sp $^{2}$ $\sigma$-bond in s-trans-1,3-butadiene.

## Conclusions

Ab initio molecular orbital theory at the $\operatorname{CCSD}(\mathrm{T}) / \mathrm{CBS}$ level plus additional corrections have been used to predict the $\sigma$ - and $\pi$-bond energies of $\mathrm{BH}_{2} \mathrm{NH}_{2}, \mathrm{AlH}_{2} \mathrm{NH}_{2}, \mathrm{BH}_{2} \mathrm{PH}_{2}$, and $\mathrm{AlH}_{2}-$ $\mathrm{PH}_{2}$. The adiabatic $\pi$-bond energy was defined as the barrier to rotation between the ground state and $C_{s}$ transition state structures, and the intrinsic $\pi$-bond energy was defined as the adiabtiac $\pi$-bond energy corrected for inversion at N or P . Using the adiabatic dissociation energies for $\mathrm{AH}_{2} \mathrm{XH}_{2}$ to $\mathrm{AH}_{2}+\mathrm{XH}_{2}$, the adiabatic $\sigma$ - and $\pi$-bond energies, respectively, for $\mathrm{BH}_{2}-$ $\mathrm{NH}_{2}$ are 109.8 and $29.9 \mathrm{kcal} / \mathrm{mol}$; for $\mathrm{AlH}_{2} \mathrm{NH}_{2}, 98.8$ and 10.5 $\mathrm{kcal} / \mathrm{mol}$; for $\mathrm{BH}_{2} \mathrm{PH}_{2}, 77.6$ and $9.2 \mathrm{kcal} / \mathrm{mol}$; and for $\mathrm{AlH}_{2}{ }^{-}$ $\mathrm{PH}_{2}, 68.3$ and $2.7 \mathrm{kcal} / \mathrm{mol}$. These results are consistent with the binding being best described as breaking a $\sigma$-bond in an $\mathrm{NH}_{2} \mathrm{R}$ or $\mathrm{PH}_{2} \mathrm{R}$ molecule that contains a delocalized lone pair (a dative $\pi$-bond). The energy differences between the weak dative $\sigma$-bond energies in $\mathrm{AH}_{3} \mathrm{XH}_{3}$ compounds and the strong $\mathrm{sp}^{2}$-sp ${ }^{2} \sigma$-bonds in the $\mathrm{AH}_{2} \mathrm{XH}_{2}$ compounds are an important reason why $\mathrm{H}_{2}$ can readily be released from $\mathrm{AH}_{3} \mathrm{XH}_{3}$ compounds (except for $\mathrm{BH}_{3} \mathrm{PH}_{3}$ ) in contrast to $\mathrm{C}_{2} \mathrm{H}_{6}$ where loss of $\mathrm{H}_{2}$ is substantially endothermic.

Acknowledgment. We thank Professor A. Arduengo, III, for helpful discussions. Funding provided in part by the Department of Energy, Office of Energy Efficiency and Renewable Energy under the Hydrogen Storage Grand Challenge, Solicitation No. DE-PS36-03GO93013. The Robert Ramsay Fund of the University of Alabama is thanked for support. This work was done as part of the Chemical Hydrogen Storage Center. This research was performed in part using the Molecular

Science Computing Facility (MSCF) in the William R. Wiley Environmental Molecular Sciences Laboratory, a national scientific user facility sponsored by the U.S. Department of Energy's Office of Biological and Environmental Research and located at the Pacific Northwest National Laboratory. Pacific Northwest National Laboratory is operated for the Department of Energy by Battelle.

Supporting Information Available: Optimized $\operatorname{CCSD}(\mathrm{T})$ geometry parameters for $\mathrm{AH}_{2}, \mathrm{XH}_{2}$, and planar $\mathrm{NH}_{3}$ and $\mathrm{PH}_{3}$, calculated vibrational frequencies, and total $\operatorname{CCSD}(\mathrm{T})$ energies $\left(E_{\mathrm{h}}\right)$ as a function of basis set extrapolated to the complete basis set limit. This material is available free of charge via the Internet at http://pubs.acs.org.

## References and Notes

(1) Gutowski, M.; Autrey, T. Prepr. Pap. - Am. Chem. Soc., Div. Fuel Chem. 2004, 49, 275.
(2) Chen, Y.; Fulton, J. L.; Linehan, J. C.; Autrey, T. J. Am. Chem. Soc. 2005, 127, 3254.
(3) Dixon, D. A.; Gutowski, M. J. Phys. Chem. A 2005, 109, 5129.
(4) Dixon, D. A.; Grant, D. J. J. Phys. Chem. A 2005, 109, 10138.
(5) Sander, S. P.; Friedl, R. R.; Ravishankara, A. R.; Golden, D. M.; Kolb, C. E.; Kurylo, M. J.; Huie, R. E.; Orkin, V. L.; Molina, M. J.; Moortgat, G. K.; Finlayson-Pitts, B. J. Chemical Kinetics and Photochemical Data for Use in Atmospheric Studies: Evaluation Number 14; JPL Publication 02-25, National Aeronautics and Space Administration, Jet Propulsion Laboratory, California Institute of Technology: Pasadena, California, 2003. http://jpldataeval.jpl.nasa.gov/pdf/JPL_02-25_rev02.pdf.
(6) Ervin, K. M.; Gronert, S.; Barlow, S. E.; Gilles, M. K.; Harrison, A. G.; Bierbaum, V. M.; DePuy, C. H.; Lineberger, W. C.; Ellison, G. B. J. Am. Chem. Soc. 1990, 112, 5750.
(7) Nicolaides, A.; Borden, W. T. J. Am. Chem. Soc. 1991, 113, 6750. Wang, S. Y.; Borden, W. T. J. Am. Chem. Soc. 1989, 111, 7282.
(8) Carter, E. A.; Goddard, W. A., III J. Am. Chem. Soc. 1988, 110, 4077. Carter, E. A.; Goddard, W. A., III J. Phys. Chem. 1986, 90, 998.
(9) Dobbs, K. D.; Hehre, W. J. Organometallics 1986, 5, 2057.
(10) Schimdt, M. W.; Truong, P. N.; Gordon, M. S. J. Am. Chem. Soc. 1987, 109, 7.
(11) Douglas, J. E.; Rabinovitch, B. S.; Looney, F. S. J. Chem. Phys. 1955, 23, 315.
(12) Allen, T. L.; Fink, W. H. Inorg. Chem. 1993, 32, 4230.
(13) Swallen, J. D., Ibers, J. A. J. Chem. Phys. 1962, 36, 1914.
(14) McKee, M. I. J. Phys. Chem. 1992, 96, 5380.
(15) Allen, T. L.; Scheiner, A. C.; Schaefer, H. F. Inorg. Chem. 1990, 29, 1930.
(16) Allen, T. L.; Fink, W. H. Inorg. Chem. 1992, 31, 1703.
(17) Marynick, D. S.; Dixon, D. A. J. Phys. Chem. 1982, 86, 914.
(18) Coolidge, M. B.; Borden, W. T. J. Am. Chem. Soc. 1990, 112, 1704.
(19) Fink, W. H.; Power, P. P.; Allen, T. L. Inorg. Chem. 1997, 36, 1431.
(20) Davy, R. D.; Jaffrey, K. L. J. Phys. Chem. 1994, 98, 8930.
(21) (a) Peterson, K. A.; Xantheas, S. S.; Dixon, D. A.; Dunning, T. H., Jr. J. Phys. Chem. A. 1998, 102, 2449. (b) Feller, D.; Peterson, K. A. J. Chem. Phys. 1998, 108, 154. (c) Dixon, D. A.; Feller, D. J. Phys. Chem. A 1998, 102, 8209. (d) Feller, D.; Peterson, K. A. J. Chem. Phys. 1999, 110, 8384. (e) Feller, D.; Dixon, D. A. J. Phys. Chem. A 1999, 103, 6413. (f) Feller, D. J. Chem. Phys. 1999, 111, 4373. (g) Feller, D.; Dixon, D. A. J. Phys. Chem. A 2000, 104, 3048. (h) Feller, D.; Sordo, J. A. J. Chem. Phys. 2000, 113, 485. (i) Feller, D.; Dixon, D. A. J. Chem. Phys. 2001, 115, 3484. (j) Dixon, D. A.; Feller, D.; Sandrone, G. J. Phys. Chem. A 1999, 103, 4744. (k) Ruscic, B.; Wagner, A. F.; Harding, L. B.; Asher, R. L.; Feller, D.; Dixon, D. A.; Peterson, K. A.; Song, Y.; Qian, X.; Ng, C.; Liu, J.; Chen, W.; Schwenke, D. W. J. Phys. Chem. A 2002, 106, 2727. (1) Feller, D.; Dixon, D. A.; Peterson, K. A. J. Phys. Chem. A, 1998, 102, 7053. (m) Dixon, D. A.; Feller, D.; Peterson, K. A. J. Chem. Phys. 2001, 115, 2576
(22) Purvis, G. D., III; Bartlett, R. J. J. Chem. Phys. 1982, 76, 1910.
(23) Raghavachari, K.; Trucks, G. W.; Pople, J. A.; Head-Gordon, M. Chem. Phys. Lett. 1989, 157, 479.
(24) Watts, J. D.; Gauss, J.; Bartlett, R. J. J. Chem. Phys. 1993, 98, 8718.
(25) Dunning, T. H., Jr. J. Chem. Phys. 1989, 90, 1007.
(26) Kendall, R. A.; Dunning, T. H., Jr.; Harrison, R. J. J. Chem. Phys. 1992, 96, 6796.
(27) McQuarrie, D. A. Statistical Mechanics; University Science Books: Sausalito, CA, 2001.
(28) Curtiss, L. A.; Raghavachari, K.; Redfern, P. C.; Pople, J. A. J. Chem. Phys. 1997, 106, 1063.
(29) Werner, H.-J.; Knowles, P. J.; Amos, R. D.; Bernhardsson, A.; Berning, A.; Celani, P.; Cooper, D. L.; Deegan, M. J. O.; Dobbyn, A. J.; Eckert, F.; Hampel, C.; Hetzer, G.; Korona, T.; Lindh, R.; Lloyd, A. W.; McNicholas, S. J.; Manby, F. R.; Meyer, W.; Mura, M. E.; Nicklass, A.; Palmieri, P.; Pitzer, R. M.; Rauhut, G.; Schütz, M.; Stoll, H.; Stone, A. J.; Tarroni, R.; Thorsteinsson, T. MOLPRO-2002; Universität Stüttgart: Stüttgart, Germany and University of Birmingham: Birmingham, United Kingdom, 2002.
(30) Rittby, M.; Bartlett, R. J. J. Phys. Chem. 1988, 92, 3033.
(31) Knowles, P. J.; Hampel, C.; Werner, H.-J. J. Chem. Phys. 1994, 99, 5219.
(32) Deegan, M. J. O.; Knowles, P. J. Chem. Phys. Lett. 1994, 227, 321.
(33) (a) Møller, C.; Plesset, M. S. Phys. Rev. 1934, 46, 618. (b) Pople, J. A.; Binkley, J. S.; Seeger, R. Int. J. Quantum Chem., Quantum Chem. Symp. 1976, 10, 1.
(34) Frisch, M. J.; Trucks, G. W.; Schlegel, H. B.; Scuseria, G. E.; Robb, M. A.; Cheeseman, J. R.; Montgomery, J. A., Jr.; Vreven, T.; Kudin, K. N.; Burant, J. C.; Millam, J. M.; Iyengar, S. S.; Tomasi, J.; Barone, V.; Mennucci, B.; Cossi, M.; Scalmani, G.; Rega, N.; Petersson, G. A.; Nakatsuji, H.; Hada, M.; Ehara, M.; Toyota, K.; Fukuda, R.; Hasegawa, J.; Ishida, M.; Nakajima, T.; Honda, Y.; Kitao, O.; Nakai, H.; Klene, M.; Li, X.; Knox, J. E.; Hratchian, H. P.; Cross, J. B.; Bakken, V.; Adamo, C.; Jaramillo, J.; Gomperts, R.; Stratmann, R. E.; Yazyev, O.; Austin, A. J.; Cammi, R.; Pomelli, C.; Ochterski, J. W.; Ayala, P. Y.; Morokuma, K.; Voth, G. A.; Salvador, P.; Dannenberg, J. J.; Zakrzewski, V. G.; Dapprich, S.; Daniels, A. D.; Strain, M. C.; Farkas, O.; Malick, D. K.; Rabuck, A. D.; Raghavachari, K.; Foresman, J. B.; Ortiz, J. V.; Cui, Q.; Baboul, A. G.; Clifford, S.; Cioslowski, J.; Stefanov, B. B.; Liu, G.; Liashenko, A.; Piskorz, P.; Komaromi, I.; Martin, R. L.; Fox, D. J.; Keith, T.; Al-Laham, M. A.; Peng, C. Y.; Nanayakkara, A.; Challacombe, M.; Gill, P. M. W.; Johnson, B.; Chen, W.; Wong, M. W.; Gonzalez, C.; Pople, J. A. Gaussian 03, revision C.02; Gaussian, Inc.: Wallingford, CT, 2004.
(35) Dunning, T. H., Jr.; Peterson, K. A.; Wilson, A. K. J. Chem. Phys. 2001, 114, 9244.
(36) Peterson, K. A.; Woon, D. E.; Dunning, T. H., Jr. J. Chem. Phys. 1994, 100, 7410.
(37) Peterson, K. A.; Dunning, T. H., Jr. J. Chem. Phys. 2002, 117, 10548. Woon, D. E.; Dunning, T. H., Jr. J. Chem. Phys. 1993, 98, 1358.
(38) Davidson, E. R.; Ishikawa, Y.; Malli, G. L. Chem. Phys. Lett.. 1981, 84, 226.
(39) Moore, C. E. Atomic energy levels as derived from the analysis of optical spectra, U. S. National Bureau of Standards Circular 467, U. S. Department of Commerce, National Technical Information Service, COM-72-50282, Washington, D. C., 1949; Vol 1.
(40) Chase, M. W., Jr.; NIST-JANAF Tables (4 ${ }^{\text {th }}$ Edition), J. Phys. Chem. Ref. Data, Mono. 9, Suppl. 1, 1998.
(41) Urdahl, R. S.; Bao, Y.; Jackson, W. M. Chem. Phys. Lett. 1991, 178, 425.
(42) Jacox, M. E. J. Phys. Chem. Ref. Data, Monograph 3, 1994.
(43) Feller, D.; Dixon, D. A.; Peterson, K. A. J. Phys. Chem. A 1998, 102, 7053
(44) Pauling, L. The Nature of the Chemical Bond, 3rd ed.; Cornell University Press: Ithaca, NY, 1960; p 271ff.
(45) Structure of Free Polyatomic Molecules - Basic Data; Kutchitsu, K., Ed.; Spronger-Verlag: Berlin, Germany, 1998.
(46) Kveseth, K.; Seip, R.; Kohl, D. Acta Chem. Scand. A 1980, 34, 31. Craig, N. C.; McKean, D. C.; Groner, P. J. Phys. Chem. A 2006, 110, 7461.
(47) McKean, D. C.; Craig, N. C.; Panchenko, Y. N. J. Phys. Chem. A 2006, 110, 8044.

